

Mark Scheme (Results)

Summer 2016

Pearson Edexcel GCE in Further Pure Mathematics 1 (6667/01)



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- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

General Instructions for Marking

- 1. The total number of marks for the paper is 75
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- **M** marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol $\sqrt{}$ will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- d... or dep dependent
- indep independent
- dp decimal places
- sf significant figures
- * The answer is printed on the paper or ag- answer given
- _ or d... The second mark is dependent on gaining the first mark

- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft.
- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
 - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
 - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.

General Principles for Further Pure Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

Method mark for solving 3 term quadratic:

1. Factorisation

 $(x^2+bx+c) = (x+p)(x+q)$, where |pq| = |c|, leading to $x = \dots$

 $(ax^2+bx+c) = (mx+p)(nx+q)$, where |pq| = |c| and |mn| = |a|, leading to x = ...

2. Formula

Attempt to use the correct formula (with values for a, b and c).

3. Completing the square

Solving $x^2 + bx + c = 0$: $\left(x \pm \frac{b}{2}\right)^2 \pm q \pm c = 0$, $q \neq 0$, leading to $x = \dots$

Method marks for differentiation and integration:

1. Differentiation

Power of at least one term decreased by 1. ($x^n \rightarrow x^{n-1}$)

2. Integration

Power of at least one term increased by 1. ($x^n \rightarrow x^{n+1}$)

<u>Use of a formula</u>

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

<u>Method mark</u> for quoting a correct formula and attempting to use it, even if there are small errors in the substitution of values.

Where the formula is <u>not</u> quoted, the method mark can be gained by implication from <u>correct</u> working with values, but may be lost if there is any mistake in the working.

Exact answers

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

Question Number	Scheme	Ма	rks
1.	Determinant of A = $(1-k)(1+k) - k^2 = 0$	M1	
	$1 - k + k - k^2 - k^2 (= 0)$	A1	
	$1 - 2k^2 (= 0)$		
	So $k = \frac{\pm\sqrt{2}}{2}$	A1	(3)
		3 r	narks
	Notes		
M	: for attempting $ad - bc = 0$ with '=0' seen or used later in the solution.		
A1	: Correct (unsimplified) expression on LHS or correct equation after brackets expanded.		
A1	: Accept $\pm \frac{\sqrt{2}}{2}$, $\pm \frac{1}{\sqrt{2}}$, $\pm \sqrt{\frac{1}{2}}$, $\pm \sqrt{0.5}$. Must have \pm for mark.		

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Question Number	Scheme	Marks
2.	(a) $f'(x) = \frac{9}{2}x^{\frac{1}{2}} + \frac{25}{2}x^{-\frac{3}{2}}$	M1 A1
		(2)
	(b) $f(12.5)=0.5115$ (at least 0.51) and $f'(12.5)=16.1927$ (at least 16 seen)	B1, B1
	$x_1 = 12.5 - \frac{f(12.5)}{f'(12.5)} = 12.5 - \frac{0.5115}{16.1927} = 12.468$	M1 A1 (4)
		6 marks
	Notes	
(a) M	1: for attempting differentiation i.e. decrease a power by 1	
	Accept equivalent expression i.e. condone equivalent fractions.	
(b) B1	: One correct, must be explicitly seen if final answer incorrect, may be implied by correct	et final
	swer.	
	B1: Both correct; must be explicitly seen if final answer incorrect, may be implied by correct final answer.	
M1: for attempting Newton- Raphson with their values for $f(12.5)$ and $f'(12.5)$		
	A1: cao correct to 3dp	
Newto	n Raphson used more than once – isw.	

Question Number	Scheme	Marks
3.	(a) $\sum_{r=1}^{3n} r^2 = \frac{1}{6} 3n(3n+1)(6n+1)$ or $\sum_{r=1}^{3n} r^2 = \frac{1}{2}n(3n+1)(6n+1)$ or equivalent	B1 (1)
	(b) See $\sum_{r=1}^{2n} r^2 = \frac{1}{3}n(2n+1)(4n+1)$ or equivalent	B1
	Attempt to use $\sum_{r=1}^{3n} r^2 - \sum_{r=1}^{2n} r^2 = \frac{n}{6} \{3(3n+1)(6n+1) - 2(2n+1)(4n+1)\}$	M1
	$=\frac{n}{6}\left\{(54n^2+27n+3)-(16n^2+12n+2)\right\}$	dM1
	$= \frac{n}{6} \{ (38n^2 + 15n + 1) \}$	A1
	(a = 38, b = 15, c = 1)	
		(4)
		5 marks
	Notes	<u> </u>
(a) B1	: Either right hand side or exact equivalent - isw if expanded	
(b) B1	: States or uses $\sum_{r=1}^{2n} r^2 = \frac{1}{3}n(2n+1)(4n+1)$	
M	: Subtracts their sum to $2n$ or $2n - 1$ and attempts to factorise by $\frac{n}{6}$ seen anywhere.	
dM	11: Expands two quadratics dependent on first M1 : cao	

Question Number	Scheme	Marks
4.	(a) $z = \frac{4(1-i)}{(1+i)(1-i)}$	M1
	z = 2(1-i) or $2 - 2i$ or exact equivalent.	A1 (2)
	(b) $z^2 = (2-2i)(2-2i) = 4-8i+4i^2$	M1
	= -8i	A1 cao (2)
	(c) If z is a root so is z^* So $(x-2+2i)(x-2-2i)$ (or $x^2 - 2\operatorname{Re}(z).x + z ^2$)	M1
	So $(x-2+2i)(x-2-2i) = 0$ (or $x^2 - 2\operatorname{Re}(z).x + z ^2 = 0$) and so $p = q =$	M1
	Equation is $x^2 - 4x + 8 (= 0)$ or $p = -4$ and $q = 8$	A1 (3) (7 marks)
ALT 1	(c) Substitutes $z = 2 - 2i$ and $z^2 = -8i$ into quadratic and equates real and imaginary parts to obtain $2p + q = 0$ and $-2p - 8 = 0$ Attempts to solve simultaneous equations to obtain $p = -4$ and $q = 8$	M1 M1A1
ALT 2	(c) Attempts to obtain $p = -$ sum of roots Attempts product of roots to obtain $q =$	M1 M1
	Equation is $x^2 - 4x + 8 = 0$ or $p = -4$ and $q = 8$	A1
ALT 3	(c) $x - 2 = \pm 2i$ either sign acceptable	M1
	$(x-2)^2 = -4 \Rightarrow x^2 - 4x + 4 = -4$ i.e square and attempt to expand to give 3-term quadratic	M1
	Equation is $x^2 - 4x + 8 (= 0)$ or $p = -4$ and $q = 8$	A1
(a)	Notes M1: Multiplies numerator and denominator by $1 - i$ or by $-1 + i$	
	: cao	
(b)	M1: Squares their z, or the given $z = \frac{4}{1+i}$, to produce at least 3 terms which can be in	nplied by the
	rect answer. : -8i or 0-8i only	
	M1: Uses their z and z^* in $(x-z)(x-z^*)$	
M	: Multiplies two factors and obtains $p = \text{ or } q =$	
	: Both correct required – can be implied by $x^2 - 4x + 8$	
(c)	T 1 M1: Substitutes their z and their z^2 into the quadratic and equates real and imaginary p prequations in p and a	parts to obtain
	two equations in p and q M1: Attempts to solve for one unknown to obtain $p = \text{ or } q =$	
	: Both correct required – can be implied by $x^2 - 4x + 8 (= 0)$	

Question Number	Scheme	Marks
5.	(a) Gradient = $\frac{2ap - 2aq}{ap^2 - aq^2}$ seen	B1
	$\left(\frac{2ap-2aq}{ap^2-aq^2} = \frac{2a(p-q)}{a(p-q)(p+q)}\right) = \frac{2}{p+q}$ or seen in an equation	B1
	uses $y - y_1 = m(x - x_1)$ to give $(y - 2aq) = "m"(x - aq^2)$ or equivalent with p	M1
	or uses $y = mx + c$ to give $y = "m"x + c$ and substitute a point to find c	
	or uses $\frac{y-y_1}{y_2-y_1} = \frac{x-x_1}{x_2-x_1}$ to give $\frac{(y-2aq)}{2ap-2aq} = \frac{(x-aq^2)}{ap^2-aq^2}$ or equivalent with p	
	so $(y-2aq) = \frac{2}{p+q}(x-aq^2)$ or $(y-2ap) = \frac{2}{p+q}(x-ap^2)$ or $y = \frac{2}{p+q}x + \frac{2apq}{p+q}$ or	A1
	$\frac{(y-2aq)}{2a} = \frac{(x-aq^2)}{a(p+q)}$	
	See $2aq^2$ or $2ap^2$ term appear and disappear to give $y(p+q) = 2x + 2apq *$	A1 cso (5)
	(b) Substitute (a, 0) into line equation, to give $0 = 2a + 2apq$ so $pq = -1$	B1 (1)
	(c) $y = 2a^{\frac{1}{2}}x^{\frac{1}{2}} \Rightarrow \frac{dy}{dx} = a^{\frac{1}{2}}x^{-\frac{1}{2}}$ or $y^2 = 4ax \Rightarrow 2y\frac{dy}{dx} = 4a$ or	M1
	$\frac{dy}{dx} = \frac{dy}{dp} \times \frac{dp}{dx} \Longrightarrow \frac{dy}{dx} = 2a \times \frac{1}{2ap}$	
	So at <i>P</i> tangent gradient = $\frac{1}{p}$	A1 (2)
	(d) At Q tangent gradient = $\frac{1}{q}$	B1
	$\frac{1}{p} \times \frac{1}{q} = \frac{1}{pq} = \frac{1}{-1} = -1$ with at least one intermediate step, the tangents are	B1cso (2)
	perpendicular or at right angles	(10 marks)
(a) B1	: Correct statement for gradient (isw) B1: $\frac{2}{p+q}$ - can be seen later in the solution.	
Must b	se of a correct formula for a line equation through P or Q with their gradient. be finding a chord, not a tangent or a normal.	
A1: cs	r a correct line equation with simplified gradient in any equivalent form o (as given answer)	
(c) M1	: For using $(a, 0)$ to show that $pq = -1$ l: Use calculus to find an expression for dy/dx and substitute coordinates of <i>P</i> . may use chord gradient and let <i>p</i> tend to <i>q</i> .	
(d) B	1: $1/q$ seen B1: $\frac{1}{p} \times \frac{1}{q} = -1$ or $\frac{1}{p} = -\frac{1}{1/q}$ or $\frac{1}{q} = -\frac{1}{1/p}$ and at least words in bold with no	errors seen.

Question Number	Scheme	Marks
6.	(a) Rotation ,135 degrees or $\frac{3\pi}{4}$ radians (anticlockwise) about <i>O</i> or 225 degrees or	M1, A1
	- 4	(2)
	$\frac{5\pi}{4}$ clockwise about <i>O</i> .	
	(b) $\begin{pmatrix} -\frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{pmatrix} \begin{pmatrix} p \\ q \end{pmatrix} = \begin{pmatrix} 6\sqrt{2} \\ 3\sqrt{2} \end{pmatrix}$	
	-p-q=12 and $p-q=6$ or equivalent	M1A1
	$p = -3$ and $q = -9$ or $\begin{pmatrix} -3 \\ -9 \end{pmatrix}$	B1 cso (3)
	ALT Uses Inverse matrix \mathbf{P}^{-1} with vector = $\begin{pmatrix} -\frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{pmatrix} \begin{pmatrix} 6\sqrt{2} \\ 3\sqrt{2} \end{pmatrix}$	M1A1
	$p = -3$ and $q = -9$ or $\begin{pmatrix} -3 \\ -9 \end{pmatrix}$	B1 cso (3)
	$(\mathbf{c}) \mathbf{Q} = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	B1 (1)
	Accept T if used instead of R	(1)
	(d) $\mathbf{R} = \mathbf{Q} \mathbf{P} = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} -\frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{pmatrix} = \begin{pmatrix} \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{pmatrix}$	M1 A1 A1 (3)
	(e) $\mathbf{R}^{-1} = \frac{1}{-1} \begin{pmatrix} -\frac{1}{\sqrt{2}} & +\frac{1}{\sqrt{2}} \\ +\frac{1}{\sqrt{2}} & +\frac{1}{\sqrt{2}} \end{pmatrix} = \begin{pmatrix} \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{pmatrix}$	
	$= \mathbf{R}$ (so matrix is self inverse and so transformation is self inverse)	B1 (1)
		10 marks
	ALT 1 (e) $\mathbf{R}\mathbf{R} = \begin{pmatrix} \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{pmatrix} \begin{pmatrix} \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$ (so R is self inverse and so transformation is self inverse)	B1
	ALT 2 (e) Matrix represents a reflection (so is self inverse)	B1
	Notes	
· · ·	M1: Rotation only A1: 135 degrees about <i>O</i> C: 135 degrees about <i>O</i> only award M1A0.	
(b)	M1: Multiplies matrices in correct order to obtain two equations in p and q .	
A1	: Two correct equations	

B1 cso: p and q both correct, may be in vector form. No errors seen in solution.

ALT (b) M1: Attempt to find Inverse Matrix and pre-multiply A1: Correct Inverse Matrix used

B1 cso: p and q both correct, may be in vector form. No errors seen in solution.

(d) M1: Sets matrix product correct way round and obtains one correct term for their **Q**

A1: Two correct terms from a correct **Q**. **Q** incorrect award A0 here. A1: Completely correct matrix (e) B1: Calculates \mathbf{R}^{-1} and indicates that $\mathbf{R}^{-1} = \mathbf{R}$ or calculates \mathbf{R}^2 and indicates that $\mathbf{R}^2 = \mathbf{I}$ or states that \mathbf{R} represents a reflection.

	Scheme	Marks
7.	(a) $z^2 = (a+2i)(a+2i) = (a^2-4)+4ia$ So $z^2 + 2z = (a^2-4+2a)+i(4a+4)$ or $x = (a^2+2a-4)$ and $y = 4a+4$ (b) and so $4a+4=0 \rightarrow a = -1$ ALT (b) Substitute $a = -1$ and show that $y = 0$ (c) $ z = \sqrt{5}$ or awrt 2.24 $\arctan(-2) = 2.03$	M1 M1 A1 A1 (4 B1 (1 B1 B1 M1, A1 cao (3
	(d) $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	M1 A1 B1ft (3
	(e) OP and QR are parallel, and QR is twice the length of OP Or Enlargement with Scale Factor 2 (centre O), followed by translation $\begin{pmatrix} -3 \\ -4 \end{pmatrix}$ Or Enlargement with Scale Factor 2, centre (3,4) or centre 3 + 4i $\overline{QR} = 2\overline{OP}$ with clear indication of vectors award B1B1, without vectors award B0B1	B1, B1 (2 13 marks
	Notes:	

Question	Scheme	Marks
Number	Scheme	IVIDI NS
8.	(i) If $n = 1$, $\sum_{r=1}^{n} \frac{2r+1}{r^2(r+1)^2} = \frac{3}{4}$ and $1 - \frac{1}{(n+1)^2} = \frac{3}{4}$, so true for $n = 1$.	B1
	Assume result true for $n = k$ and consider $\sum_{r=1}^{k+1} \frac{2r+1}{r^2(r+1)^2} = 1 - \frac{1}{(k+1)^2} + \frac{2(k+1)+1}{(k+1)^2(k+2)^2}$	M1
	$=1 - \left(\frac{(k+2)^2}{(k+1)^2(k+2)^2} - \frac{2(k+1)+1}{(k+1)^2(k+2)^2}\right) = 1 - \left(\frac{(k^2+2k+1)}{(k+1)^2(k+2)^2}\right)$	A1
	$=1 - \left(\frac{(k+1)^2}{(k+1)^2(k+2)^2}\right) = 1 - \left(\frac{1}{(k+1+1)^2}\right)$	M1
	True for $n = k + 1$ if true for $n = k$, (and true for $n = 1$) so true by induction for all	A1cso
	$n \in Z^+$	(5)
l	(ii) $n = 1$: $u_1 = 5 \times \left(\frac{1}{3}\right)^1 + \frac{4}{3} = 3$ so expression for u_n true for $n = 1$	B1
	Assume result true for $n = k$ and consider $u_{k+1} = \frac{1}{3}(5 \times (\frac{1}{3})^k + \frac{4}{3}) + \frac{8}{9}$	M1
	Obtain $u_{k+1} = 5 \times \left(\frac{1}{3}\right)^{k+1} + \frac{4}{9} + \frac{8}{9}$	A1
	$5 \times \left(\frac{1}{3}\right)^{k+1} + \frac{4}{3}$ and deduce that result is true for $n = k+1$	dM1
	True for $n = k + 1$ if true for $n = k$, (and true for $n = 1$) so true by induction for all $n \in Z^+$	A1 cso (5)
		10 marks

Notes:

(i) B1: Checks n = 1 on both sides **and** states true for n = 1 seen anywhere M1: (Assumes true for) n = k and adds (k+1)th term to sum of k terms

A1:
$$1 - \left(\frac{(k^2 + 2k + 1)}{(k+1)^2(k+2)^2}\right)$$
 seen (linked to 2nd M)

M1: $(k+1)^2(k+2)^2$ attempted as common denominator of two fractions.

A1cso: Makes correct complete induction statement including at least statements in bold. Accept $n \ge 1$ or n = 1, 2, 3... or all positive Integers or all *n*. Statement true for n = 1 here could contribute to B1 mark earlier. (ii) B1: Checks n = 1 in u_n and states true for n = 1 seen anywhere.

M1: (Assumes result for) n = k and substitutes u_k into correct expression for u_{k+1}

A1:
$$\frac{4}{9} + \frac{8}{9}$$
 or $\frac{1}{3} \cdot \frac{4}{3} + \frac{8}{9}$ seen
dM1: Obtains $5 \times \left(\frac{1}{3}\right)^{k+1} + \frac{4}{3}$ and statement true for $n = k + 1$ or equivalent seen anywhere dependent on

previous M.

A1cso: Makes correct complete induction statement including at least statements in bold. Accept $n \ge 1$ or n = 1, 2, 3... or all positive Integers or all n. Statement true for n = 1 here could contribute to B1 mark earlier.

Question Number	Scheme	Marks
	$y = \frac{25}{x} \Longrightarrow \frac{dy}{dx} = -25x^{-2} ,$	B1
	or $y + x \frac{dy}{dx} = 0 \Rightarrow \frac{dy}{dx} = -\frac{y}{x}$ or $\dot{x} = 5$, $\dot{y} = -\frac{5}{t^2}$ so $\frac{dy}{dx} = -\frac{1}{t^2}$	
	and at $P = \frac{dy}{dx} = -\frac{1}{p^2}$ so gradient of normal is p^2	M1 A1
	Either $y - \frac{5}{p} = p^2(x - 5p)$ or $y = p^2 x + k$ and use $x = 5p$, $y = \frac{5}{p}$	M1
	$\Rightarrow \qquad y - p^2 x = \frac{5}{p} - 5p^3 \tag{(*)}$	A1cso (5
(b)	At the point A: $y + p^2 y = \frac{5}{p} - 5p^3$ or $-x - p^2 x = \frac{5}{p} - 5p^3$	
	$y(1+p^2) = \frac{5}{p}(1-p^4)$ or $-x(1+p^2) = \frac{5}{p}(1-p^4)$	M1
	$y = \frac{\frac{5}{p}(1-p^2)(1+p^2)}{(1+p^2)} = \frac{5}{p}(1-p^2) = \frac{5}{p}-5p \text{ or } x = \frac{-\frac{5}{p}(1-p^2)(1+p^2)}{(1+p^2)} = \frac{-5}{p}(1-p^2) = \frac{-5}{p}+5p *$	M1
	so $x = -\frac{5}{p}(1-p^2) = -\frac{5}{p} + 5p$ and $y = \frac{5}{p} - 5p^*$	A1cso (3
(c)	<i>M</i> has coordinates $\left(-\frac{5}{2p}+5p, \frac{5}{p}-\frac{5p}{2}\right)$ o.e.	B1
	So when $y = 0$, $\frac{5}{n} - \frac{5p}{2} = 0$ and $p = \sqrt{2}$ so <i>M</i> has <i>x</i> coordinate $\frac{15}{4}\sqrt{2}$ o.e.	M1 A1
	p 2 4	(11 marks
	Notes	
	B1: Any correct expression for gradient of tangent: Substitutes values into derived expression using calculus to give gradient of normal at <i>P</i>	
A1	: cao. Can be implied by use in equation of a straight line	
	: Use of formula for the equation of a straight line with their changed gradient : cso	
(b)	M1: Replaces x by $-y$ or y by $-x$	
	: Factorises $(1 - p^4)$ to simplify answer in first variable	
	cso: Obtains both x and y T (b) Accept Verification	

ALT (b) Accept Verification.

M1: Substitutes the coordinates of *A* into the equation of the normal M1: Substitutes the coordinates of *A* into both the normal and y = -x.

A1 cso: No errors seen

(c) B1: Correct *x*- coordinate of midpoint (may be implied) and correct *y* coordinate, accept equivalent forms M1: Puts their y = 0 and finds value for *p* to use in x =

A1: $+\frac{15}{4}\sqrt{2}$ or equivalent only

PMT

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